Musical Source Separation: Principles and State of the Art

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Presentation overview

I. Introduction

- o Paradigms, tasks, applications
- Mixing models
- 2. Solving the linear mixing model
 - o Joint and staged separation
- 3. Estimation of the mixing matrix
 - The need for sparsity
 - o Independent Component Analysis
 - o Clustering methods, other methods
- 4. Estimation of the sources
 - Norm minimization
 - o Time-frequency masking
- 5. Methods using advanced source models
 - o Adaptive basis decomposition methods
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 - o Supervised methods
- 6. Conclusions

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Sound Source Separation

- "Cocktail party effect"
 - o E. C. Cherry, 1953.
 - Ability to concentrate attention on a specific sound source from within a mixture.
 - Even when interfering energy is close to energy of desired source.
- "Prince Shotoku Challenge"
 - Legendary Japanese prince Shotoku (6th Century AD) could listen and understand simultaneously the petitions by ten people.
 - Concentrate attention on several sources at the same time!
 - o "Prince Shotoku Computer" (Okuno et al., 1997)
- Both allegories imply an extra step of semantic understanding of the sources, beyond mere acoustical isolation.

[Cherry53] E. C. Cherry. Some Experiments on the Recognition of Speech, With One and Two Ears. Journal of the Acoustical Society of America, Vol. 25, 1953.

[Okuno97] H. G. Okuno, T. Nakatani and T. Kawabata. Understanging Three Simultaneous Speeches. Proc. Int. Joint Conference on Artificial Intelligence (IJCAI), Nagoya, Japan, 1997.





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Musical Source Separation.

The paradigms of Musical Source Separation

- (based on [Scheirer00])
 - Understanding without separation
 - Multipitch estimation, music genre classification
 - "Glass ceiling" of traditional methods (MFCC, GMM) [Aucouturier&Pachet04]
 - Separation for understanding
 - First (partially) separate, then feature extraction
 - Source separation as a way to break the glass ceiling?
 - Separation without understanding
 - BSS: Blind Source Separation (ICA, ISA, NMF)
 - Blind means: only very general statistical assumptions taken.
 - Understanding for separation
 - Supervised source separation (based on a training database)

[Scheirer00]E. D. Scheirer. Music-Listening Systems. PhD thesis, Massachusetts Institute of Technology, 2000.[Aucouturier&Pachet04]J.-J. Aucouturier and F. Pachet. Improving Timbre Similarity: How High is the Sky? Journal of Negative Results in Speech
and Audio Sciences, 1 (1), 2004.

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Required sound quality

- Regarding the quality of the separated sounds, source separation tasks can be divided into:
- Audio Quality Oriented (AQO)
 - Aimed at full unmixing at the highest possible quality.
 - Applications:
 - o Unmixing, remixing, upmixing
 - o Hearing aids
 - o Post-production
- Significance Oriented (SO)
 - Separation quality just enough for facilitating semantic analysis of complex signals.
 - o Less demanding, more realistic.
 - Applications:
 - o Music Information Retrieval
 - o Polyphonic Transcription
 - o Object-based audio coding

Musical Source Separation Tasks

• Classification according to the nature of the mixtures:

	Source position	Mixing process	Source/mixture ratio	Noise	Musical texture	Harmony
- Difficulty +	 changing static	 echoic (changing impulse response) echoic (static impulse response) delayed instantaneous 	underdeterminedoverdeterminedeven-determined	noisynoiseless	 monodic (multiple voices) heterophonic homophonic / homorhythmic polyphonic / contrapuntal monodic (single voice) 	 tonal atonal

Classification according to available a priori information:

	Source position	Source model	Number of sources	Type of sources	Onset times	Pitch knowledge
- Difficulty +	 unknown statistical model known mixing matrix 	 none statistical independence sparsity advanced/trained source models 	unknownknown	unknownknown	 unknown known (score/MIDI available) 	 none pitch ranges score/MIDI available

+ A priori knowledge -

Linear mixing model

• Only amplitude scaling before mixing (summing)

$$x_{m}(t) = \sum_{n=1}^{N} a_{mn} s_{n}(t), \quad m = 1, \dots, M.$$
$$\begin{pmatrix} x_{1}(t) \\ x_{2}(t) \\ \vdots \\ x_{M}(t) \end{pmatrix} = \begin{pmatrix} a_{11} & a_{12} & \dots & a_{1N} \\ a_{21} & a_{22} & \dots & a_{2N} \\ \vdots & \vdots & \ddots & \vdots \\ a_{M1} & a_{M2} & \dots & a_{MN} \end{pmatrix} \cdot \begin{pmatrix} s_{1}(t) \\ s_{2}(t) \\ \vdots \\ s_{N}(t) \end{pmatrix}$$

• Linear stereo recording setups:



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Delayed mixing model

• Amplitude scaling and delay before mixing

$$x_m(t) = \sum_{n=1}^N a_{mn} s_n(t - \delta_{mn}), \qquad m = 1, \dots, M. \qquad \mathbf{A} = \begin{pmatrix} a_{11}\delta(t - \delta_{11}) & \dots & a_{1N}\delta(t - \delta_{11}) \\ \vdots & \ddots & \vdots \\ a_{M1}\delta(t - \delta_{M1}) & \dots & a_{MN}\delta(t - \delta_{MN}) \end{pmatrix}$$
$$\mathbf{x} = \mathbf{A} * \mathbf{s}$$

Delayed stereo recording setups:



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Convolutive mixing model

• Filtering between sources and sensors

$$x_{m}(t) = \sum_{n=1}^{N} h_{mn}(t) * s_{n}(t) = \sum_{n=1}^{N} \sum_{k=1}^{K_{mn}} a_{mnk} s_{n}(t - \delta_{mnk}), \quad m = 1, \dots, M. \qquad \mathbf{A} = \begin{pmatrix} n_{11}(t) & \dots & n_{1N}(t) \\ \vdots & \ddots & \vdots \\ h_{M1}(t) & \dots & h_{MN}(t) \end{pmatrix}$$
$$\mathbf{x} = \mathbf{A} * \mathbf{S}$$

• Convolutive stereo recording setups:



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Some terminology

- System of linear equations: $\mathbf{X} = \mathbf{AS}$
 - o Usual algebraic methods from high school: ${f X}$ known, ${f A}$ known, ${f S}$ unknown
 - $_{\rm 0}$ But in source separation: unknown variables (S, sources) AND unknown coefficients (A, mixing matrix)
- Algebra terminology is retained for source separation:
 - More equations (mixtures) than unknowns (sources): overdetermined
 - o Same number of equations (mixtures) than unknowns (sources): determined (square A)
 - o Less equations (mixtures) than unknowns (sources): underdetermined
- The underdetermined case is the most demanding, but also the most important for music!
 - Music is (still) mostly in stereo, with usually more than 2 instruments
 - Overdetermined and determined situtations are only of interest for arrays of sensors or arrays of microphones (localization, tracking)
- Alternative interpretation of the linear model as a linear transform from signal space to mixture space, with A the transformation matrix and the columns of A the transformation bases.

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Solving the linear model

- Direct way to tackle the problem:
 - Mean Square Error (MSE) minimization: $\min_{\mathbf{A},\mathbf{S}} \|\mathbf{X} \mathbf{AS}\|_F^2$
 - o F is the Frobenius norm ("matrix energy")
 - o BUT: this has infinitely many solutions
- One must assume probability distributions for the involved variables
 - o Maximum A Posteriori (MAP) approach: maximize $P(\mathbf{A}, \mathbf{S} | \mathbf{X})$
 - o Applying Bayes' theorem $P(\mathbf{A},\mathbf{S}|\mathbf{X}) = \frac{P(\mathbf{X}|\mathbf{A},\mathbf{S})P(\mathbf{A})P(\mathbf{S})}{P(\mathbf{X})}$ and
 - Assuming A has a uniform distribution (all source positions are equally equal) and
 - o Assuming the sources are statistically independent this finally yields

$$\min_{\mathbf{A},\mathbf{S}} \left\{ \frac{1}{2\sigma^2} \left\| \mathbf{X} - \mathbf{AS} \right\|_F^2 - \sum_{n,t} l_n(s_n(t)) \right\}$$

o σ^2 is the noise variance (if any) and l_n is the assumed log-density of the sources

Staged separation

- However, such a joint estimation of A and S is:
 - o Extremely computationally demanding
 - o Unstable with respect to convergence
- Most methods follow thus a staged approach: first estimate the mixing matrix, then estimate the sources.



• Note that, if A is square (determined source separation) and invertible (virtually always for usual mixtures), then the sources can be readily obtained by $\hat{\mathbf{S}} = \hat{\mathbf{A}}^{-1}\mathbf{X}$

(^ denotes estimation)

- In that case, source separation amounts to mixing matrix estimation!
- In the underdetermined case, A is rectangular and thus non-invertible. Thus, a second source estimation stage is needed!

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Mixing matrix estimation

• Simple examples can be visualized by means of scatter plots





> Underdetermined mixture (2 channels, 3 sources)

- The coordinates of each data point are the values of a certain signal coefficient (time sample, time-frequency bin) in each of the mixtures.
- Data points tend to concentrate around the vectors defined by the columns of the mixing matrix: the mixing directions.
- The goal of mixing matrix estimation is thus to find such vectors.

The need for sparsity

- A signal is said to be sparse if most of its coefficients (in some domain) are zero or close to zero.
- Sparse signals will have a peaked probability distribution.
 - Example: Laplacian signals are sparser than Gaussian signals

Laplace distribution: $p(c) = \frac{\lambda}{2}e^{-\lambda|c-\mu|}$



- Geometrical perspective:
 - The sparser the signals, the more their coefficients will be concentrated around the mixing directions, and the easier will be the detection of the directions.
- Analytical perspective:
 - o Remember the MAP problem:

$$\min_{\mathbf{A},\mathbf{S}} \left\{ \frac{1}{2\sigma^2} \| \mathbf{X} - \mathbf{AS} \|_F^2 + \sum_{n,t} l_n(s_n(t)) \right\}$$

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Penalty for sparsity

- Measures of sparsity
 - o L1-norm

o Kurtosis L1-norm:
$$\|\mathbf{c}\|_1 = \sum_{i=1}^{n} |c_i|$$

o Negentropy

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How to increase sparsity

- Time-frequency domain much sparser than time domain
 - Short Time Fourier Transform (STFT)
- Logarithmic resolution front-ends
 - o Constant-Q Transform (CQT)
 - o Discrete Wavelet Transform (DWT)
- Auditory resolution front-ends
 - o Bark
 - o ERB (Equal Rectangular Bandwidth)
 - o Mel
- Adaptive signal decompositions
 - o Basis Pursuit
 - o Matching Pursuit

Spectrogram (|STFT|)





Independent Component Analysis (1)

• ICA tries to find the mixing directions by aligning the coefficient clusters to the (orthogonal) scatter axes.



- Note that Principal Component Analysis (PCA), which finds the directions of greatest variance, is not enough for the alignment.
- However, PCA is used as a first step for ICA because, when followed by whitening (variance normalization), it makes the mixing directions orthogonal, and thus ICA reduces to finding the remaining rotation.
- Also, note that this is only possible for determined mixtures \rightarrow not very useful for music!
- Axis alignment corresponds to the sources being statistically independent.

Independent Component Analysis (II)

- ICA works by maximizing some objective measure of statistical independence between candidate sources.
- Methods based on maximizing nongaussianity of the sources
 - FastICA based on kurtosis or negentropy
- Methods based on minimizing mutual information between sources
- Methods based on Maximum Likelihood (ML) estimation
 - o Bell-Sejnowski (BS) algorithm
 - o Natural gradient algorithm
 - FastICA based on ML
- Tensorial methods ("decorrelate" higher order statistics)
 - o FOBI (Fourth-Order Blind Identification)
 - o JADE (Joint Approximate Diagonalization of Eigenmatrices)
- Sound examples (Hyvärinen et al.)



Hyvärinen + Karhunen + Oja



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Clustering methods

- Explore the mixture space to find the clusters.
- Allow underdetermined separation!
- Direct inspection of the scatter plot: sparsity is crucial!
- Example: kernel-based angular clustering
 - o [Bofill&Zibulevsky01]
 - o Kind of smoothed histogram

Mixture scatter and found directions



• Also: methods based on k-Means, fuzzy C-means clustering...

[Bofill&Zibulevsky01] P. Bofill and M. Zibulevsky. Underdetermined Blind Source Separation Using Sparse Representations. Signal Processing, Vol. 81, 2001.

Other methods for mixing matrix estimation

- Phase cancellation methods
 - ADRess (Azimuth Discrimination and Resynthesis) [Barry04]
 - Artificial stereo panning retains phase and only changes amplitude between channels → phase cancellation in the interchannel difference spectrogram



(Fig. from [Barry04])

- Methods from image processing applied to the scatter plots
 - Example: application of the Hough transform to detect straight lines created by the direction clusters [Lin97]
- [Barry04] D. Barry, B. Lawlor and E. Coyle. Sound Source Separation: Azimuth Discrimination and Resynthesis. Proc. Int. Conf. on Digital Audio Effects (DAFX), Naples, Italy, 2004.
- [Lin97] J. K. Lin, D. G. Grier and J. D. Cowan. Feature Extraction Approach to Blind Source Separation. Proc. IEEE Workshop on Neural Networks for Signal Processing (NNSP), 1997.

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- Norm minimization
- o Time-frequency masking

Source estimation by norm minimization

- In the underdetermined case, A is rectangular and thus non-invertible. Thus, a second source estimation stage is needed!
- Norm minimization methods
 - o Recall (again) the minimization problem $\min_{\mathbf{A},\mathbf{S}} \left\{ \frac{1}{2\sigma^2} \|\mathbf{X} \mathbf{AS}\|_F^2 \sum_{n,t} l_n(s_n(t)) \right\}$
 - Assuming no noise, known A and Laplacian (sparse) sources, this simplifies to an L1-norm minimization problem:

$$\hat{\mathbf{S}} = \operatorname{argmin}_{\mathbf{X} = \hat{\mathbf{A}}\mathbf{S}} \left\{ \sum_{n,t} |s_n(t)| \right\}$$

- o A realization thereof is the shortest-path algorithm
- Sound examples for angular kernel clustering plus shortest-path estimation:





Time-frequency masking (I)

• Goal: find a mask M that retrieves one source when used to filter a given time-frequency representation.

$$\hat{\mathbf{S}}_n(r,k) = \mathbf{M}_{mn}(r,k) \circ \mathbf{X}_m(r,k)$$



- Adaptive Wiener filtering
- Binary time-frequency masking
 - DUET (Degenerate Unmixing Estimation Technique) [Yilmaz&Rickard04]
 - Histogram of Interchannel Intensity (IID) and Phase (IPD) Differences
 - Binary Mask created by selecting bins around histogram peaks.



• is the Hadamard (element-wise) product

Drawback of t-f masking: "musical noise" or "burbling" artifacts

[Yilmaz&Rickard04] Ö. Yilmaz and S. Rickard. Blind Separation of Speech Mixtures via Time-Frequency Masking. IEEE Trans. on Signal Processing. Vol. 52(7), July 2004

Time-frequency masking (2)

- Human-assisted time-frequency masking [Vinyes06]
 - Human-assisted selection of the time-frequency bins out of the DUETlike histogram for creating the unmixing mask
 - o Implementation as a VST plugin ("Audio Scanner")





[Vinyes06] M. Vinyes, J. Bonada and A. Loscos. Demixing Commercial Music Productions via Human-Assisted Time-Frequency Masking. *120th AES convention*, Paris, France, 2006.

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 - o Adaptive basis decomposition methods
 - o Sinusoidal methods
 - Supervised methods

Advanced source models methods

- Until now: blind approaches (only general, statistical assumptions)
- The use of (sometimes music-specific) advanced source models allow to improve separation quality and to handle highly underdetermined situations (e.g. separation from mono mixtures)
- Classification according to a priori knowledge
 - o Supervised
 - o Based on training the model with a sound example database
 - o Better quality and more demanding situations at the cost of less generality
 - o Unsupervised
- Classification according to model type
 - o Adaptive basis decompositions (ISA, NMF, NSC)
 - o Sinusoidal Modeling
- Classification according to mixture type
 - o Monaural systems
 - o Hybrid systems combining advanced source models with spatial diversity

Independent Subspace Analysis

- Application of ISA to audio: Casey and Westner, 2000.
- Application of ICA to the spectogram of a mono mixture.
- Each independent component corresponds to an independent subspace of the spectrogram.



- Component-to-source clustering
 - The extracted components usually do not directly correspond to the sources.
 - They must be clustered together according to some similarity criterion.
 - Casey&Westner use a matrix of Kullback-Leibler divergences called the ixegram.

[Casey&Westner00] M. Casey and A. Westner. Separation of Mixed Audio Sources by Independent Subspace Analysis. Proc, Int. Computer Music Conference (ICMC), Berlin, Germany, 2000.

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Nonnegative Matrix Factorization

- Matrix factorization ($\mathbf{X} = \mathbf{AS}$) imposing non-negativity.
- Needed when using magnitude or power spectrograms.
- NMF does not aim at statistical independence, but:
 - It has been proven that, under some conditions, non-negativity is sufficient for separation.
 - NMF yields components that very closely correspond to the sources.
 - To date, there is no exact theoretical explanation why is that so!
- Use for transcription:
 - P. Smaragdis and J.C. Brown. Non-Negative Matrix Factorization for Polyphonic Music Transcription. Proc. IEEE Workshop on Applications of Signal Processing to Audio and Acoustics (WASPAA), New Paltz, USA, 2003.
- Use for separation:
 - B. Wang and M. D. Plumbley. Musical Audio Stream Separation by Non-Negative Matrix Factorization. *Proc. UK Digital Music Research Network (DMRN) Summer Conf.*, 2005.

Nonnegative Sparse Coding

- Combination of non-negativity and sparsity constraints in the factorization.
- [Virtanen03]: NSC is optimized with an additional criterion of temporal continuity.
 - Measured by the absolute value of the overall amplitude difference between consecutive frames.



- [Virtanen04]: Convolutive Sparse Coding
 - Improved temporal accuracy by modeling the sources as the convolution of spectrograms with a vector of onsets.

$$(M_n)_{t,f} = \left(\sum_{n=1}^{N} [a_n \otimes s_{n,f}]\right)_t$$

Mixture O Component I C Component 2

- [Virtanen03] T. Virtanen. Sound Source Separation Using Sparse Coding with Temporal Continuity Objective. Proc. Int. Computer Music Conference (ICMC), Singapore, 2003.
- [Virtanen04] T. Virtanen. Separation of Sound Sources by Convolutive Sparse Coding. Proc. ISCA Tutorial and Research Workshop on Statistical and Perceptual Audio Processing (SAPA), Jeju, Korea, 2004.

Sinusoidal Methods

- Sinusoidal Modeling: detection and tracking of the sinusoidal partial peaks on the spectrogram.
- Based on Auditory Scene Analysis (ASA) cues of good-continuation, common fate and smoothness of sinusoidal tracks.
- Overall, very good reduction of interfering sources, but moderate timbral quality.
- Generation of the second secon



- Appropriate for Significance-Oriented applications
- [Virtanen&Klapuri02]: model of spectral smoothness of harmonic sounds
 - Based on basis decomposition of harmonic structures
 - o Additive resynthesis of partial parameters
- [Every&Szymanski06]
 - o Spectral subtraction instead of additive resynthesis

[Virtanen&Klapuri02]	T. Virtanen and A. Klapuri. Separation of Harmonic Sounds Using Linear Models for the Overtone Series. Proc.
	IEEE Int. Conf. on Acoustics, Speech and Signal Processing (ICASSP), Orlando, USA, 2002.
[Every&Szymanski06]	M. R. Every and J. E. Szymanski. Separation of Synchronous Pitched Notes by Spectral Filtering of Harmonics.
	IEEE Trans. on Audio, Speech and Signal Processing. Vol. 14(5), 2006.

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Separated

sources

Mixture 🜔

Supervised Methods (I)

- Use of a training database to create a set of source models, each one modeling a specific instrument.
 - Better separation as a trade-off for generality.
- Supervised sinusoidal methods
 - o [Burred&Sikora07]
 - The source models are compact descriptions of the spectral envelope and its temporal evolution.
 - The detailed temporal evolution allows to ignore harmonicity constraints, and thus separation of chords and inharmonic sounds is possible.

sources



sources

Separation of chordsInharmonic separationImage: SeparatedInharmonic separationImage: SeparatedImage: SeparatedImage: SeparatedImage: SeparatedImage: SeparatedImage: Separated



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Supervised Methods (2)

Bayesian Networks

- o [Vincent06]
- Multilayered model describing note probabilities (state layer), spectral decomposition (source layer) and spatial information (mixture layer).
- o Trained on a database of isolated notes.
- o Allows separation of sounds with reverb.
- Learnt priors for Wiener-based separation
 - o [Ozerov05]
 - o Single-channel
 - HMM models of singing voice and accompaniment.



- [Vincent06] E. Vincent. Musical Source Separation Using Time-Frequency Source Priors. *IEEE Trans. on Audio, Speech and Language Processing,* Vol. 14 (1), 2006.
- [Ozerov05] A. Ozerov, O. Philippe, R. Gribonval and F. Bimbot. One Microphone Singing Voice Separation Using Source-Adapted Models. Proc. IEEE Workshop on Applications of Signal Processing to Audio and Acoustics (WASPAA), New Paltz, USA, 2005.

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Conclusions

- Still far from fully-general, audio-quality-oriented system.
- More realistic: significance oriented
 - Separation good enough to facilitate content analysis
- Methods based on adaptive models, time-frequency masking:
 - More realistic mixtures, but more artifacts and interferences
- Methods based on sinusoidal modeling:
 - More artificial timbre, but less interferences.
- Current polyphony limitations:
 - o Mono signals: up to 3, 4 instruments
 - o Stereo signals: up to 5, 6 instruments

Literature

- Very few overview materials on Musical Source Separation
- P. D. O'Grady, B. A. Pearlmutter and S. T. Rickard. Survey of sparse and non-sparse methods in source separation. International Journal of Imaging Systems and Technology, 15(1). 2005.
- E. Vincent, M. G. Jafari, S. A. Abdallah, M. D. Plumbley and M. E. Davies.
 Model-based audio source separation. Technical Report C4DM-TR-05-01, Queen Mary University, London, UK, 2006.
- T. Virtanen. Unsupervised Learning Methods for Source Separation in Monaural Music Signals. Chapter in A. Klapuri, M. Davy (Eds.), Signal Processing Methods for Music Transcription, Springer 2006.

• Stereo Audio Source Separation Evaluation Campaign:

http://sassec.gforge.inria.fr